

# Propensity Score의 소개와 이용

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## 예제

Hospital Type	Severity of Illness		
	Mild (Mortality Rate %)	Severe (Mortality Rate %)	Total (Mortality Rate %)
World-Class Hospitals	3/327 (1%)	41/678 (6%)	44/1,005 (4.4%)
Local Hospitals	8/258 (3%)	3/33 (9%)	11/291 (3.8%)
Total	11/585 (2%)	44/711 (3%)	

- sever 환자가 큰 병으로 가다. 사망률은 큰 병에서 더 높다.
- Treatment selection이 severity와 독립이 아니다.
- 병의 비교에 있어서 severity는 중요한 혼란변수.
- Typical “Apples to Oranges” comparisons

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- Typical “Apples to Oranges” comparisons

## Limitations of Random Assignment

- Large RCTs take a long time and great cost to generate answers—analysis of existing data may more timely, yet acceptably accurate
- RCTs are not feasible when variables cannot be manipulated—e.g., some events in child welfare are driven by legal mandates
- Prior analysis of the need for withholding treatment should be done before RCTs are deemed necessary.

## Propensity Score Analysis

- Motivation
  - Control for a large number of confounders by adjusting for a single summary variable
- Propensity Score
  - Predicts the probability of receiving the intervention as a function of the confounders

propensity score matching AND kidney - PubMed result Page 1 of 3

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1 Long-term clinical outcomes following drug-eluting or bare-metal stent placement in patients with severely reduced CFS: Results of the Massachusetts Data Registry Center. *Mass Cardiovasc Stroke Registry*.  
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2 Surgical versus conservative management for multistage disease in patients with acute coronary syndrome: analysis from the ACUTE (Acute Coronial Intervention and Long-term Intervention) Trial. *Stroke*.  
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5 Cognitive function and progression of mild neurocognitive impairment: analysis of the Alzheimer's Disease Neuroimaging Initiative. *Alzheimer Dis Assoc*.  
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7 Effects of oral statin 100 mg HDL on long-term outcomes after percutaneous transluminal angioplasty in patients with hemoperitoneal disease undergoing hemodialysis: a retrospective cohort study in Japanese patients. *BMC Nephrol*.  
Ishi H, Kimura Y, Toyoyama T, Aoyama T, Takahashi H, Tanaka M, Kameo D, Kawamura Y, Yamada S, Hayashi M, Yasuda T, Huzawa Y, Maruyama S, Matsuo S, Mitsuhashi T, Maruyama T.  
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PMID: 19782868 PubMed - indexed for MEDLINE Free Article

## What are propensity scores?

- is the predicted probability of an outcome (SUGI 29;165)
- is generally defined as the conditional probability of assignment to a particular treatment given a vector of observed covariates (Rosenbaum and Rubin 1983)
- are the predicted probabilities from a logistic model which models the probabilities of being in the various levels of the predictor of primary interest as a function of a set of secondary variables.

## Propensity Scores

- Suppose we want to look at a response (expression of a certain outcome) if a patient received a treatment, compared to the response if the patient did not receive the treatment.
- Dataset we wish to have

Patient	Outcome if received treatment	Outcome if received no treatment	Treatment impact
A	12	8	4
B	7	4	3
C	7	3	4
D	12	9	3

## Propensity Scores

- What is in reality?

Patient	Outcome if received treatment	Outcome if received no treatment	Treatment impact
A	12	?	?
B	7	?	?
C	?	3	?
D	?	9	?

## Propensity Scores

- The question is ...
  - If we have a patient who got the treatment in the dataset, how can we specify what that patient's response would have been if they had not gotten the treatment?
  - The treatment effect is the difference between the two responses (treatment – no treatment)
  - Rubin Causal Model – potential outcomes framework

## Propensity Scores

- Comparing apples to apples

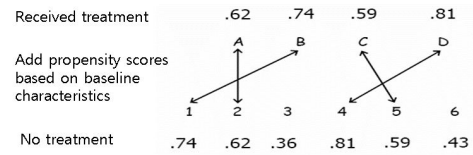
## Propensity Scores

- Propensity scores
  - We have a lot of information on each potential subject.
    - Demographics
    - Geographic/socioeconomic information
  - We can estimate the probability that a subject with these background characteristics will receive the treatment.

$$0 \leq PS \leq 1$$

## Propensity Scores

- Comparing apples to apples



## Propensity Scores

- The new dataset, simply

Patient	Propensity to get treatment	Outcome if received treatment	Outcome if received no treatment	Treatment impact
A	0.8	12	9	3
B	0.5	7	3	4
C	0.5	7	3	4
D	0.8	12	9	3

- Match A to D and B to C and plug in resulting estimates for blanks...

## General Procedure

### Run Logistic Regression:

- Dependent variable: Y=1, if participate; Y = 0, otherwise.
- Choose appropriate conditioning (instrumental) variables.
- Obtain propensity score: predicted probability (p) or  $\log[(1-p)/p]$ .

### Match each Participant to One or More Nonparticipants on Propensity Score

- Nearest neighbor matching
- Caliper matching
- Mahalanobis Metric matching in conjunction with PSM
- stratification (subclassification)
- Difference-in-differences matching (Kernel & local linear weights (Heckman))

Multivariate analysis based on new sample

Introduction to Propensity Score Matching  
By Shenyang Guo, Ph.D. (sguo@mail.unc.edu)  
School of Social Work, University of North Carolina at Chapel Hill

## Calculation of Propensity Score

- Propensity scores are generally calculated using one of two methods:

1. **Logistic regression:** This is the most commonly used method for estimating propensity scores.
2. **Classification and Regression Tree Analysis(CART):** It is a model used to predict the probability that an event occurs.

### •Requirement

1. classification ability : **C statistic**
  - Treatment 영향의 PS에 ROC curve를 그렸을 때 AUC
  - 0.75이상이면 만족
2. calibration ability: **Hosmer-Lameshow test**
  - LR model에 Goodness-of-fit test
  - p가 significant level이 아니면 만족.

## Classification and Regression tree analysis (CART)

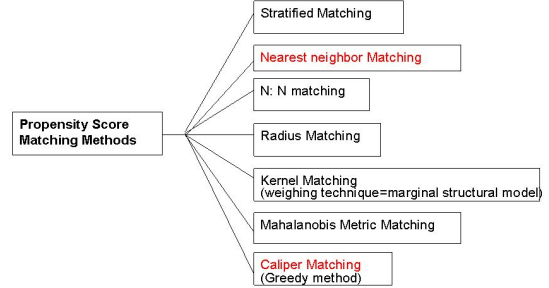
- This is a **non-parametric decision tree method** that can efficiently partition populations into homogenous subgroups (Lemon, Freidmann, Rakowski, 2003).
- It is **not as widely used as logistic regression for estimating propensity scores** (because it is complex and more suitable for use by those with a statistical background)

## Adjustment for the estimated propensity scores

- Adjustment for the estimated propensity scores is accomplished using one or a combination of the four main methods.
  - (1) Stratification,
  - (2) **Matching**,
  - (3) Covariate/Regression adjustment, and
  - (4) Weighting
- Once the propensity scores are estimated, these methods can be used to estimate the treatment effect after adjusting for differences between the treatment groups.
- Both stratification and matching are used to adjust for the covariate **before** calculating the treatment effect. In contrast, regression adjustment is used **while** determining the treatment effect.

## Propensity Score Matching Methods

Once researchers obtain an estimated propensity score, an appropriate matching technique is implemented.



## Nearest Neighbor and Caliper Matching

- Nearest neighbor:**
  - Randomly order the participants and nonparticipants, then select the first participant and find the nonparticipant with closest propensity score
- Caliper**
  - define a common-support region (e.g., .01 to .00001), and randomly select one nonparticipant that matches on the propensity score with the participant.
  - SAS macro "**GREEDY**" does this.
- 1-to-1 Nearest neighbor within caliper** (common practice)
- 1-to-n Nearest neighbor within caliper**

Introduction to Propensity Score Matching  
By Shenyang Guo, Ph.D. (sguo@email.unc.edu)  
School of Social Work, University of North Carolina at Chapel Hill

## Stratification

One of several methods developed for missing data imputation

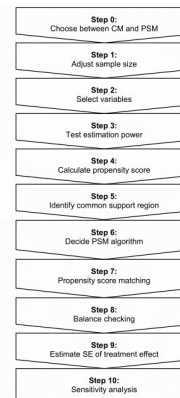
- Group sample into five categories based on propensity score (quintiles).
- Within each quintile, there are  $r$  participants and  $n$  nonparticipants. Use "approximate Bayesian bootstrap" method to conduct matching or resampling.

## Multivariate Analysis

- We could perform any kind of multivariate analysis we originally wished to perform on the unmatched data. These analyses may include:
- multiple regression
  - generalized linear model
  - survival analysis
  - structural equation modeling with multiple-group comparison, and
  - hierarchical linear modeling (HLM)

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## PSM implementation steps



CM: Covariate matching  
PSM: Propensity score matching  
SE: Standard error

Yang et al.

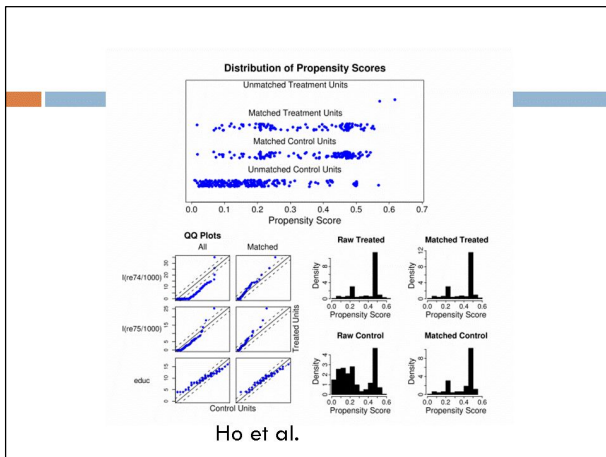
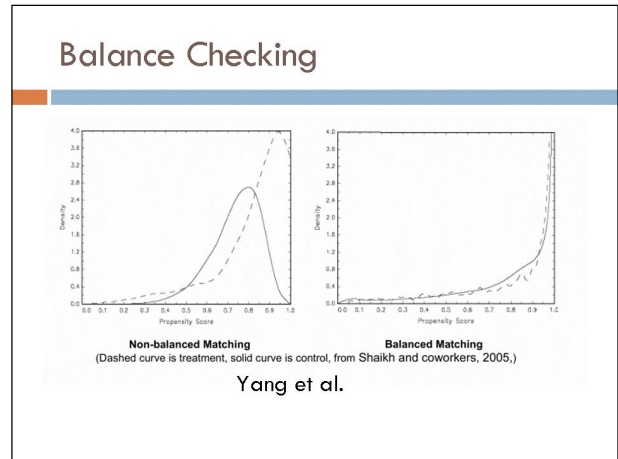
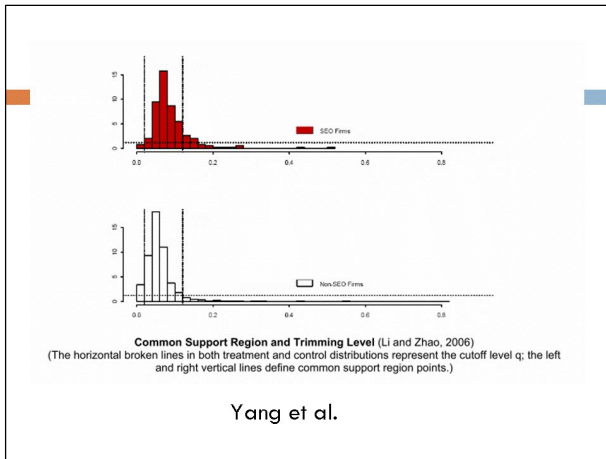


Table 2: 1:1 Matched Population				
	Treatment N (%)	No Treatment N (%)	p-value	
<b>Total Patients</b>	<b>3,905</b>	<b>3,905</b>		
Age	Mean ± sd	67.1 ± 12.3	66.8 ± 13.7	0.5596
Female	1,481 (37.9)	1,468 (37.6)	0.7616	
White Race	3,283 (84.1)	3,259 (83.9)	0.4515	
ECG Obtained	300 (7.7)	278 (7.2)	0.2820	
Sex to Diasthr	Mean ± sd	2.2 ± 2.0	2.2 ± 2.2	0.1327
Hx Angina	483 (12.4)	479 (12.3)	0.9205	
Hx MI	872 (22.3)	888 (22.7)	0.9448	
Hx CHF	259 (6.6)	243 (6.2)	0.4604	
Hx CABG	340 (8.7)	331 (8.5)	0.7163	
Hx PICA	511 (13.1)	506 (13.0)	0.8665	
Hx Diabetes	931 (23.8)	931 (23.8)	0.7505	
Hx Smoking	1,155 (29.4)	1,122 (28.7)	0.4855	
Hx Hyperchol	1,116 (28.6)	1,110 (28.4)	0.8805	
Hx CAD	963 (24.7)	950 (24.3)	0.7323	
Hx Hyperten	2,360 (60.6)	2,388 (61.2)	0.2665	
Hx Stroke	1,475 (37.8)	1,454 (37.2)	0.6296	
Hx Renal	118 (3.0)	125 (3.2)	0.8311	
Hx COPD	293 (7.5)	291 (7.5)	0.3439	
Chest Pain	3,401 (88.1)	3,411 (88.6)	0.4846	
Philip Score IV	183 (4.7)	187 (4.8)	0.8313	
Systolic BP	Mean ± sd	139.8 ± 35.6	141.0 ± 37.0	0.8313
Diastolic BP	Mean ± sd	80.7 ± 20.5	81.2 ± 20.9	0.5005
Pulse	Mean ± sd	81.5 ± 23.3	82.0 ± 23.0	0.1378
Propensity Score	Mean ± sd	0.064, 0.883	0.064, 0.876	
	min, max			

Table 3: 1:2 Matched Population				
	Treatment N (%)	No Treatment N (%)	p-value	
<b>Total Patients</b>	<b>2,164</b>	<b>4,328</b>		
Age	Mean ± sd	71.7 ± 10.9	72.5 ± 11.7	0.0001
Female	978 (45.1)	1,946 (44.96)	0.9157	
White Race	1,833 (84.7)	3,652 (84.3)	0.5216	
ECG Obtained	104 (4.8)	209 (4.8)	0.9673	
Sex to Diasthr	Mean ± sd	2.6 ± 2.2	2.6 ± 2.4	0.1713
Hx Angina	312 (14.4)	616 (14.2)	0.8410	
Hx MI	578 (26.7)	1,138 (26.3)	0.7022	
Hx CHF	237 (11.0)	472 (10.9)	0.8651	
Hx CABG	281 (13.0)	540 (12.5)	0.2613	
Hx PICA	213 (9.8)	391 (9.0)	0.3960	
Hx Diabetes	634 (29.3)	1,216 (28.1)	0.3120	
Hx Smoking	470 (21.7)	874 (20.2)	0.1528	
Hx Hyperchol	518 (23.9)	958 (22.1)	0.0538	
Hx CAD	462 (21.4)	892 (20.6)	0.4895	
Hx Hyperten	1,350 (62.4)	2,691 (62.2)	0.3706	
Hx Stroke	766 (35.4)	1,485 (34.3)	0.0556	
Hx Renal	106 (4.9)	201 (4.6)	0.6482	
Hx COPD	155 (7.2)	337 (7.8)	0.3706	
Chest Pain	1,683 (77.8)	3,426 (79.2)	0.1984	
Philip Score IV	107 (4.9)	175 (4.0)	0.0937	
Systolic BP	Mean ± sd	142.4 ± 36.9	142.1 ± 36.5	0.2967
Diastolic BP	Mean ± sd	80.4 ± 20.3	80.1 ± 19.8	0.5124
Pulse	Mean ± sd	87.2 ± 25.0	86.8 ± 23.6	0.2776
Propensity Score	Mean ± sd	0.064, 0.477	0.064, 0.485	
	min, max			

Parson et al.

- ### Example
- Aspirin Use and Mortality
    - 6174 consecutive adults undergoing stress echocardiography for evaluation of known suspected coronary disease.
    - 2310 (37%) were taking aspirin (treatment).
    - Main outcome: all-cause mortality
    - Median follow-up: 3.1 years
    - Univariate analysis: 4.5% of aspirin patients died, and 4.5% of non-aspirin patients died ...
    - Unadjusted hazard ratio: 1.08 (0.85, 1.39)

- ### Example
- Propensity Score Model for Aspirin Use
    - Logistic regression predicting aspirin use
    - 31 covariates included in the model
      - Demographics, clinical history, medication use
      - Cardiovascular assessment and exercise capacity
    - Estimated propensity scores for aspirin use range from 0.03 to 0.98.
    - Does the propensity score model work?
    - Are the covariates balanced?

## Example

- Baseline Characteristics by Aspirin Use (in %) (before Matching)

Variable	Aspirin (n = 2310)	No Aspirin (n = 3864)	P value
Men	77.0	56.1	< .001
Clinical history: diabetes	16.8	11.2	< .001
hypertension	53.0	40.6	< .001
prior coronary artery disease	69.7	20.1	< .001
congestive heart failure	5.5	4.6	.12
Medication use: Beta-blocker	35.1	14.2	< .001
ACE inhibitor	13.0	11.4	< .001

- Baseline characteristics appear very dissimilar: 25 of 31 covariates have  $p < .001$ , 28 of 31 have  $p < .05$ .
- Aspirin user covariates indicate higher mortality risk.

## Example

- Matching with Propensity Scores

- For each patient, we have a propensity score.
- Match to the non-user with closest propensity score (within some limit or "calipers")
- Eliminate both patients from pool, and repeat until you cannot find an acceptable match.
  - Could match a non-user with propensity score inside "calipers" who matches exactly on characteristic  $X_i$  or ...
  - Match non-user with propensity score inside "calipers" and smallest "distance" on some pre-specified covariates.

## Example

- Matching on Gender within PS calipers

- Shuffle "treatment" patients, and select one.
- Find all "non-treated" with PS inside calipers (here we set calipers at treated PS  $\pm 0.03$ )
- Match patient within calipers of same gender.
- Repeat until no more matches are possible

Patient	Exposure	PS	Gender
A	Treated	.76	Male
B	Not Treated	.77	Female
C	Not Treated	.74	Male
D	Not Treated	.80	Male

.80  
.79  
.78  
.77  
**.76**  
.75  
.74  
.73  
.72

## Example

- How Were the Aspirin Subjects Matched?

- Tried to match each aspirin user to a unique non-user with a PS identical to 5 digits.
- If not possible, proceeded to a 4-digit match, then 3-digit, 2-digit, and finally 1-digit match (i.e., propensity scores within .099).
- Result: matches for 1351(58%) of the 2310 aspirin patients to 1351 unique non-users.

## Example

- Baseline Characteristics by Aspirin Use (%) (after Matching)

Variable	Aspirin (n = 1351)	No Aspirin (n = 1351)	P value
Men	70.4	72.1	.33
Clinical history: diabetes	15.0	15.3	.83
hypertension	50.3	51.7	.46
prior coronary artery disease	48.3	48.8	.79
congestive heart failure	5.8	6.6	.43
Medication use: Beta-blocker	26.1	26.5	.79
ACE inhibitor	15.5	15.8	.79

- Baseline characteristics similar in matched users and non-users.
- 30 of 31 covariates show NS difference between matched users and non-users. [Peak exercise capacity for men is  $p = .01$ ]

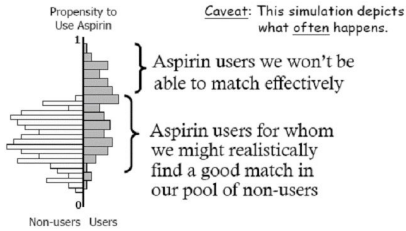
## Example

- Which Aspirin Users Get Matched?

- Generally, characteristics of unmatched aspirin users tend to indicate high propensity scores.
  - Overall 37% of patients were taking aspirin.
  - The rate was much higher in some populations... 67% of Prior CAD patients were taking aspirin.
  - So, prior CAD patients had higher propensity for aspirin.
  - 99.8% of unmatched aspirin users had prior CAD.
- Likely that unmatched users tended towards larger propensity scores than matched users.

## Example

- Who is Getting Matched Here? Where Do the Propensity Scores Overlap?



## Example

- Matching with Propensity Scores
  - 1351 aspirin subjects matched well to non-aspirin subjects – big improvement in covariate balance. Matched group looks like an RCT ...
  - Matching still incomplete, but results on PS matched group mirrored the results for the covariate-adjusted group as a whole ...
  - Resulting matched pairs analyzed using standard statistical methods, e.g. Kaplan-Meier, Cox PH models.

## Example

- Estimating the Hazard Ratios

Approach	n	Hazard Ratio	95% CI
Full sample, no adjustment	6174	<b>1.08</b>	(.85, 1.39)
Full sample with no PS, adjusted for all covariates	6174	<b>0.67</b>	(.51, .87)
PS-Matched sample	2702	<b>0.53</b>	(.38, .74)
PS-Matched, adjusted for PS and all covariates	2702	<b>0.56</b>	(.40, .78)

- During follow-up 153 (6%) of the 2702 propensity score-matched patients died.
- Aspirin use was associated with a lower risk of death in matched group (4% vs. 8%,  $p = .002$ ).

## Example

- Aspirin Conclusions / Caveats
  - Patients included in this study may be a more representative sample of "real world" patients than an RCT would provide.
  - PS matching is still not randomization: can only account for the factors measured, and only as well as the instruments can measure them.
  - No information on aspirin dose, aspirin allergy, or duration of treatment, or on medication adjustments.

## Discussion

- Advantages in PS method
  - It is useful when adjusting for a large number of confounders and small number of events per variable.
- Limitations in PS method
  - PSM cannot adjust for unobserved covariates,
  - PSM works better in larger samples, and
  - Group overlap is substantial in PSM.
  - PS model should be correct.
- PS method can be used for *missing data analysis* under missing at random(MAR) assumption.

## What should always be done in an observational study and often is not?

- Collect data so as to be able to model selection
- Demonstrate selection bias – need for PS
- Ensure covariate overlap for comparability
- Evaluate covariate balance after PS application
- Specify relevant post-adjustment population carefully
- Model or estimate treatment effect in light of PS (adjustment / matching / stratification)
- Estimate sensitivity of results to potential hidden bias.

# 예시 (1)

## The NEW ENGLAND JOURNAL of MEDICINE

ESTABLISHED IN 1812 APRIL 24, 2008 VOL. 358 NO. 17

### Stents versus Coronary-Artery Bypass Grafting for Left Main Coronary Artery Disease

Ki Bae Seung, M.D., Duk-Woo Park, M.D., Young-Hak Kim, M.D., Seung-Whan Lee, M.D., Cheol Whan Lee, M.D., Myeong-Ki Hong, M.D., Seong-Wook Park, M.D., Sung-Cheol Yun, Ph.D., Hyeon-Cheol Gwon, M.D., Myung-Ho Jeong, M.D., Yangsoo Jang, M.D., Hyo-Soo Kim, M.D., Pum Jong Kim, M.D., In-Whan Seong, M.D., Hun Sik Park, M.D., Taehoon Ahn, M.D., In-Ho Chae, M.D., Seung-Jea Tahk, M.D., Wook-Sung Chung, M.D., and Seung-Jung Park, M.D.

Table 1. Baseline Characteristics of the Patients.\*

Variable	Stent Group (N=1102)	CABG Group (N=1118)	P Value
<b>Demographic characteristics</b>			
Age (yr)	62	64	<0.001
Median	52-70	57-70	
Interquartile range	70.7	72.9	0.14
<b>Cardiac or coexisting conditions</b>			
<b>Any diabetes</b>			
Insulin-dependent	29.7	34.7	0.01
Noninsulin-dependent	4.8	8.2	0.22
Hypertension (% of patients)	49.3	49.4	0.94
Hyperlipidemia (% of patients)	38.5	32.6	0.04
Current smoker (% of patients)	25.6	29.8	0.03
Previous coronary artery bypass grafting (% of patients)	18.1	11.0	<0.001
Previous myocardial infarction (% of patients)	8.1	11.6	0.005
Previous congestive heart failure (% of patients)	2.3	5.3	0.21
Chronic obstructive pulmonary disease (% of patients)	2.0	2.0	0.97
Coronary artery disease (% of patients)	7.1	7.3	0.84
Treatment vascular disease (% of patients)	1.5	1.4	<0.001
Renal failure (% of patients)	2.7	3.0	0.71
<b>Electrocardiogram (% of patients)</b>			
Median	42	60	<0.001
Interquartile range	57-67	52-66	
<b>Electrocardiographic findings (% of patients)</b>			
Sinus rhythm	87.8	87.1	0.13
Atrial fibrillation	2.0	2.7	
Other	0.2	0.2	
<b>Clinical indication (% of patients)</b>			
Stent indication	1.0	2.2	<0.001
Chronic stable angina	12.0	10.9	
Unstable angina	35.2	38.1	
Non-Q-wave myocardial infarction	9.8	9.8	
<b>Anatomic characteristics</b>			
Involved location (% of patients)	50.4	46.2	0.04
Distal, mid, or both	49.4	53.8	
<b>Extent of distal vessel (% of patients)</b>			
Left main only	25.2	4.2	<0.001
Left main plus single-vessel disease	24.0	20.5	
Left main plus double-vessel disease	26.0	26.3	
Left main plus triple-vessel disease	24.8	37.0	
Right coronary artery disease (% of patients)	15.8	10.7	<0.001
Rotational lesion (% of patients)	2.8	1.2	0.005

## Methods of Propensity-Score Matching (1)

- The propensity scores were estimated without regard to outcome variables, using **multiple logistic-regression analysis**.
  - All prespecified covariates, which are listed in Table 1 of the article, were included in the final models for treatment with PCI versus CABG along with pertinent second-order interactions using step-wise selection procedures.
  - A propensity score was then calculated from the logistic equation for each patient.
  - Also, for each concurrent comparison (Wave 1 and Wave 2), a separate propensity score for PCI versus CABG was generated using the same method for the overall cohort and was incorporated for each analysis.
- The predictive ability of each propensity-score model was assessed by means of the C statistic (0.86 for the entire cohort, 0.88 for Wave 1, and 0.86 for Wave 2), indicating good discrimination between two treatments.

## Methods of Propensity-Score Matching (2)

- Using the **"Greedy 5→1 digit match algorithm"**, we created **propensity-score-matched pairs** without replacement (a 1:1 match).
  - Specifically, we sought to match each patient with PCI to one with CABG who had a **propensity score that was identical to 5 digits**.
  - If this could not be done, the algorithm then proceeded **sequentially to the next highest digit match (a 4-, 3-, 2-, or 1-digit) on propensity score to make "next-best" matches**, in a hierarchical sequence until no more matches could be made.
  - If a subject who received PCI could not be matched to any subject who received CABG on the first digit of the propensity score, that subject with PCI was discarded from the matched analysis.
  - Once a match was made, previous matches were not reconsidered before making the next match.
  - After all of the propensity-scores-matches were performed, we assessed the balance in baseline covariates between the two intervention groups with the paired t-test or the Wilcoxon signed rank test for continuous variables, and the McNemar's test or marginal homogeneity test for categorical variables.

Table 2. Baseline Characteristics of the Propensity-Matched Patients.\*

Variable	Overall Cohort			Wave 1†			Wave 2‡		
	Stent (N=552)	CABG (N=552)	P Value§	Stent (N=276)	CABG (N=276)	P Value§	Stent (N=276)	CABG (N=276)	P Value§
Age (yr)	64	64		61	61		64	64	
Median	56-71	56-70		51-69	53-67		57-72	58-70	
Interquartile range	71.6	71.2	0.89	71.0	71.0	0.91	71.1	71.7	0.89
<b>Cardiac or coexisting conditions</b>									
<b>Any diabetes</b>									
Insulin-dependent	32.7	33.9	0.95	28.1	28.0	0.99	36.1	34.9	0.86
Noninsulin-dependent	7.8	7.9	0.91	4.8	3.1	0.08	10.1	10.9	0.57
Hypertension (% of patients)	49.4	50.0	0.90	49.9	45.4	0.09	52.3	53.0	0.81
Hyperlipidemia (% of patients)	29.3	30.2	0.84	27.1	27.1	0.99	32.6	33.6	0.81
Current smoker (% of patients)	27.7	27.1	0.89	28.3	28.0	0.98	26.3	25.3	0.87
Previous coronary artery bypass grafting (% of patients)	14.6	15.1	0.81	14.0	14.3	0.98	15.4	15.4	0.99
Previous myocardial infarction (% of patients)	8.2	10.0	0.58	9.7	10.6	0.87	8.8	9.1	0.90
Previous congestive heart failure (% of patients)	2.8	3.0	0.99	2.4	2.9	0.99	3.0	3.1	0.99
Chronic obstructive pulmonary disease (% of patients)	2.0	2.2	0.85	2.4	2.3	0.99	2.0	2.1	0.99
Coronary artery disease (% of patients)	7.4	6.4	0.72	6.8	6.3	0.98	8.1	7.3	0.78
Treatment vascular disease (% of patients)	2.0	2.0	0.99	1.9	1.9	0.99	2.3	2.3	0.79
Renal failure (% of patients)	3.7	3.8	0.99	3.9	3.4	0.98	3.3	4.1	0.83
<b>Electrocardiogram (% of patients)</b>									
Median	41	42	0.42	42	42	0.67	40	40	0.53
Interquartile range	54-66	55-66		57-67	56-66		55-66	56-66	
<b>Electrocardiographic findings (% of patients)</b>									
Sinus rhythm	87.6	86.7	0.80	87.6	87.1	0.99	87.7	86.3	0.42
Atrial fibrillation	2.4	3.1	0.24	2.4	2.9	0.23	2.3	3.0	0.10
Other	0.9	0.2	0.01	0	0	0	0	0.3	
<b>Clinical indication (% of patients)</b>									
Stent indication	2.8	2.0	0.07	2.0	1.4	0.18	2.1	2.3	0.41
Chronic stable angina	29.2	28.4	0.44	16.4	14.4	0.11	30.1	28.3	
Unstable angina	37.4	37.9	0.86	40.6	40.6	0.99	37.6	37.6	
Non-Q-wave myocardial infarction	10.7	11.1	0.81	11.1	10.6	0.84	9.8	10.4	
<b>Anatomic characteristics</b>									
Involved location (% of patients)	48.3	47.8	0.90	62.8	62.4	0.99	19.4	18.9	0.91
Distal, mid, or both	51.7	52.2	0.82	37.2	37.6	0.94	80.6	81.1	
<b>Extent of distal vessel (% of patients)</b>									
Left main only	11.8	11.1	0.81	21.3	21.3	0.99	3.8	3.8	0.41
Left main plus single-vessel disease	17.0	16.2	0.80	29.0	29.0	0.99	12.4	11.6	
Left main plus double-vessel disease	31.2	33.9	0.39	34.9	34.9	0.99	29.9	29.9	
Left main plus triple-vessel disease	39.3	38.7	0.79	15.9	15.9	0.98	52.4	52.0	
Right coronary artery disease (% of patients)	15.7	15.7	0.99	29.1	29.1	0.99	11.9	11.9	0.44
Rotational lesion (% of patients)	1.4	1.4	0.99	1.9	2.4	0.08	1.8	1.7	0.57

\*CABG denotes coronary artery bypass grafting. Percentages may not total 100 because of rounding.  
 †Wave 1 shows comparisons between coronary artery and CABG.  
 ‡Wave 2 shows comparisons between drug-eluting stents and CABG.  
 §P values are based on the paired t-test or the Wilcoxon signed rank test for continuous variables, and on the McNemar's test or marginal homogeneity test for categorical variables.

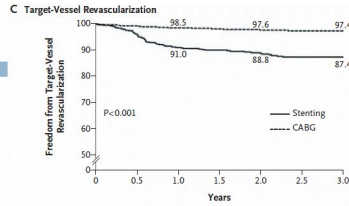


Table 3. Hazard Ratios for Clinical Outcomes after Stenting as Compared with after CABG among Propensity-Matched Patients.\*

Outcome	Overall Cohort (N=542 pairs)		Wave 1 (N=207 pairs)		Wave 2 (N=336 pairs)	
	Hazard Ratio (95% CI)	P Value	Hazard Ratio (95% CI)	P Value	Hazard Ratio (95% CI)	P Value
Death	1.18 (0.77-1.80)	0.45	1.04 (0.59-1.83)	0.90	1.36 (0.80-2.30)	0.26
Composite outcome of death, Q-wave myocardial infarction, or stroke	1.10 (0.73-1.62)	0.61	0.86 (0.50-1.49)	0.59	1.40 (0.88-2.22)	0.15
Target-vessel revascularization	4.76 (2.80-8.11)	<0.001	10.70 (3.80-29.90)	<0.001	5.96 (2.51-14.10)	<0.001

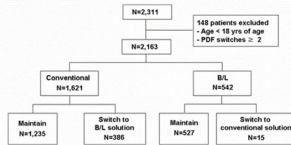
\*CABG denotes coronary-artery bypass grafting. Wave 1 shows comparisons between bare-metal stents and CABG, and Wave 2 shows comparisons between drug-eluting stents and CABG. Hazard ratios are for the stenting group as compared with the CABG group.

## 예시 (2)

### Mortality and Technique Failure in Peritoneal Dialysis Patients Using Advanced Peritoneal Dialysis Solutions

Seung Hyeok Han, MD, PhD,<sup>1,2</sup> Song Yogui Ahn, MD,<sup>3</sup> Jee Young Yun, CRN,<sup>4</sup> Anders Traaneus, MD, PhD,<sup>5</sup> and Dae-Suk Han, MD, PhD<sup>6</sup>

- conventional lactate-buffered glucose based (Dianeal<sup>®</sup>) vs. B/L buffer [biocompatible physiological-pH bicarbonate(25 mmol/L)/lactate(15 mmol/L) buffer; Physioneal<sup>®</sup>]
- 2,163 patients starting peritoneal dialysis therapy between July 2003 and December 2006 from 54 centers in Korea



Am J Kidney Dis 54:711-720. © 2009 by the National Kidney Foundation, Inc.

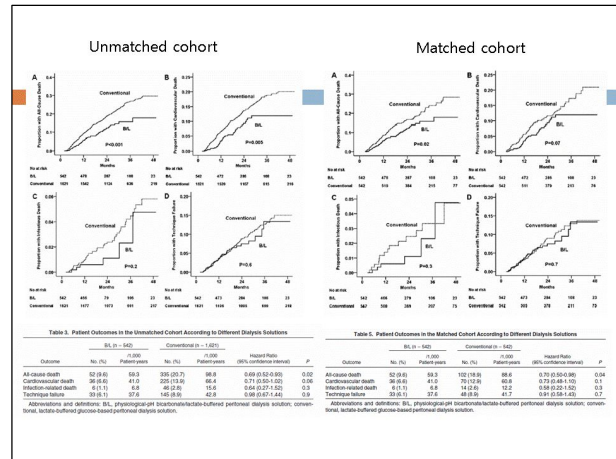


Table 4. Multivariate Cox Proportional Hazard Models for Mortality

	Unmatched Cohort		Matched Cohort	
	Hazard Ratio (95% confidence interval)	P	Hazard Ratio (95% confidence interval)	P
B/L (v conventional)	0.69 (0.52-0.93)	0.02	0.70 (0.50-0.98)	0.04
Sex (women v men)	1.16 (0.95-1.42)	0.2	1.05 (0.76-1.45)	0.8
Age (1 yr increase)	1.07 (1.06-1.08)	<0.001	1.07 (1.05-1.09)	<0.001
Diabetes (v no diabetes)	1.99 (1.58-2.49)	<0.001	1.91 (1.35-2.70)	<0.001
Cardiovascular comorbidity (v no)	1.36 (1.06-1.76)	0.02	1.31 (0.87-1.98)	0.2
Low socioeconomic status (v high)	1.16 (0.91-1.46)	0.2	1.35 (0.95-1.92)	0.1
Center (v less experienced)	0.83 (0.65-1.12)	0.2	0.49 (0.32-0.76)	0.001
Iodextrin (v no use)	0.43 (0.34-0.55)	<0.001	0.40 (0.28-0.58)	<0.001

Note: Models were adjusted for age, sex, diabetes, cardiovascular comorbidity, socioeconomic status, center experience, and iodextrin use.  
Abbreviations and definitions: B/L, physiological-pH bicarbonate/lactate-buffered peritoneal dialysis solution; conventional, lactate-buffered glucose-based peritoneal dialysis solution.

## Software Packages

- SAS: SUGI 214-26 "GREEDY" Macro
- STATA: PSMATCH2
  - (developed by Edwin Leuven and Barbara Sianesi [2003], as a user-supplied routine in STATA)
  - the most comprehensive package that allows users to fulfill most tasks for propensity score matching
- R: MatchIT
- SPSS: Matching을 하기 힘들다...

## SAS® MACROS

**%GREEDMTCH** does nearest neighbor within caliper matching. If more than one control matches to a case, the control is selected at random. No replacement is adopted in this macro.

<http://www2.sas.com/proceedings/sugi26/p214-26.pdf>

**%OneToManyMTCH** allows propensity score matching from 1-to-1 to 1-to-N based on specification from user. In use of nearest neighbor algorithm, the macro makes "best" matches first and "next-best" matches next in a hierarchical sequence until all matched controls use up. Each control can be selected once. This macro contains some ideas of greedy matching.  
<http://www2.sas.com/proceedings/sugi29/165-29.pdf>

**%Mahalanobis** and **%MATCH** was proposed by Feng and his colleges at Eli Lilly Inc. in 2006. It implements the nearest available mahalanobis metric matching within calipers determined by propensity score. The caliper is defined as one quarter of standard deviation of the logit of propensity score. **%Mahalanobis** is nested in **%MATCH** for mahalanobis distance calculation when there are more than two matched control subjects.  
<http://www.lexjansen.com/pharmasug/2006/publichealthresearch/pr05.pdf>

## SAS® MACROS

**%MATCHUP** was proposed by Martin and Ganguly, where both mahalanobis metric matching within caliper and a simple matching within caliper are provided with the caliper defined by the logit of propensity score. If processing time or capacity is a concern, a simple alternative can be performed quickly compared to the mahalanobis method at the potential price of more bias.  
<http://www.rx.uga.edu/main/home/cas/faculty/propensity.pdf>

**%BLINPLUS** was developed using a validation study containing data on the two estimated propensity scores (error-prone and gold-standard) as well as the parameter estimates, their standard errors and covariances from Cox proportional hazards model. The error-prone propensity score was estimated from immeasurable confounding factors. The macro output provides the adjusted relative hazard rate estimates, including 95% confidence intervals adjusted for additional uncertainty from the estimation of the error-prone model (Stürmer and coworkers, 2005).  
<http://www.hsph.harvard.edu/faculty/spiegelman/blinplus/blinplus8.sas>

## SAS® MACROS

**%MATCH** was developed by Bergstralh and his coworkers in 1995 and replaced by %GMATCH, %VMATCH and %DIST later. Using distance measure, this macro can be used to match 1 or more controls for each subject in the treated group by means of greedy or optimal algorithms. %MATCH worked originally on observational variables before the propensity score was introduced into the model as a matching factor.

<http://mayoresearch.mayo.edu/mayo/research/biostat/sasmacros.cfm>.

**%MCSTRAT** was developed by Vierkant and his colleges in 2000. This macro fits a conditional logistic model from matched or finely stratified data by propensity score and generates tables to describe the matching results as well as independent variables included in model. PROC PHREG and PROC IML are two major SAS procedures that perform regression diagnoses such as leverage value, delta chi-square, influential statistics and several other tools. <http://mayoresearch.mayo.edu/mayo/research/biostat/upload/65.pdf>

## S-PLUS/R PACKAGES

**Matching** by Sekhon provides functions for estimating causal effects by multivariate and propensity score matching and for finding best balance based on genetic search algorithm. The package includes a variety of univariate and multivariate tests to determine if balance has been obtained by the matching procedure. <http://jsekhon.fas.harvard.edu/matching>

**MATCHIT**. This technique matches each treated unit to all possible control units with exactly the same value on all the covariates and propensity score by a variety of matching algorithms including exact matching, subclassification matching, nearest neighbor matching, optimal matching, full matching and genetic matching. After matching, balance is checked using plot or several other tools. The imputation of missing values is done via simulation using a parametric model together with Monte Carlo estimation. The subsequent analyses based on a parametric statistical model reduces the model dependence on background noises. <http://gking.harvard.edu/matchit/docs/matchit.html>.

## S-PLUS/R PACKAGES

**OPTMATCH**. This is bipartite matching, matching algorithms fall into two categories, greedy and optimal, where the latter functions with reconsideration of previous made matches in each new step. It combines propensity score with other multivariate distances, and functions for adaptations for large and memoryintensive issues. Full matching is its core algorithm, matching ratio between treated and control can vary. <http://stat.cmu.edu/R/CRAN/doc/packages/optmatch.pdf>

**USPS**. This is one of packages developed by Ben Obenchain, containing R functions that perform a variety of alternative approaches to propensity scoring analyses. The USPS methods implement various forms of a-posteriori matching or stratification of patients who received only one of the two treatments that are being compared. <http://www.math.iupui.edu/~indyasa/>.

## S-PLUS/R PACKAGES

**Propensity score profiling (Propscore)** This software package is for comparing among multiple groups using propensity score with shrinkage estimation while addressing regression to the mean that can result from such multiple comparisons, based on Bayesian principles. [http://www.biostat.jhsph.edu/~cfrangak/papers/proscore\\_profiling/routine.r](http://www.biostat.jhsph.edu/~cfrangak/papers/proscore_profiling/routine.r)

**Twang toolkit**. Among the procedures available in the Twang toolkit, PS calculates propensity scores and diagnoses them using a variety of methods, centered on using boosted logistic regression. DIAG plot creates the diagnostic plots of propensity score; SENSITIVITY does sensitivity analysis, to name a few. <http://rss.acs.unt.edu/Rdoc/library/twang/html/00Index.html>

## Software Packages

- There is currently no commercial software package that offers formal procedure for PSM.
  - In SAS, Lori Parsons developed several Macros (e.g., the **GREEDY macro** does **nearest neighbor within caliper matching**).
  - In SPSS, Dr. John Painter of Jordan Institute developed a SPSS macro to do similar works as GREEDY (<http://sswnt5.sowo.unc.edu/VRC/Lectures/index.htm>).
- We have investigated several computing packages and found that PSMATCH2 (developed by Edwin Leuven and Barbara Sianesi [2003], as a user-supplied routine in STATA) is the most comprehensive package that allows users to fulfill most tasks for propensity score matching, and the routine is being continuously improved and updated.

## Others

**STATA: PSMATCH2**, <http://ideas.repec.org/c/boc/bocode/s432001.html>.  
**PSCORE, ATTND, ATTNW, ATTR, ATTS AND ATTK**, [http://www.labor-torino.it/pdf\\_doc/fichino.pdf](http://www.labor-torino.it/pdf_doc/fichino.pdf) **MATCH**  
<http://elsa.berkeley.edu/~imbens/statamatching.pdf>

**SPSSPropensityMatching Macro**, <http://sswnt5.sowo.unc.edu/VRC/Lectures/index.htm>

**S-plus with FORTRAN Routine**

## Limitations of Propensity Scores

- Large samples are required
- Group overlap must be substantial
- Hidden bias may remain because matching only controls for observed variables (to the extent that they are perfectly measured)

(Shadish, Cook, & Campbell, 2002)

## Criteria for “Good” PSM

- Identify treatment and comparison groups with substantial overlap
- Match, as much as possible, on variables that are precisely measured and stable (to avoid extreme baseline scores that will regress toward the mean)
- Use a composite variable—e.g., a propensity score—which minimizes group differences across many scores